Q. No. 1 – 25 Carry One Mark Each

1. Consider the following statements regarding the complex Poynting vector \( \mathbf{\mathbf{P}} \) for the power radiated by a point source in an infinite homogeneous and lossless medium. \( \mathbf{Re}(\mathbf{P}) \) denotes the real part of \( \mathbf{P} \). \( S \) denotes a spherical surface whose centre is at the point source, and \( \mathbf{n} \) denotes the unit surface normal on \( S \). Which of the following statements is TRUE?

(A) \( \mathbf{Re}(\mathbf{P}) \) remains constant at any radial distance from the source

(B) \( \mathbf{Re}(\mathbf{P}) \) increases with increasing radial distance from the source

(C) \( \iiint_{S} \mathbf{Re}(\mathbf{P}) \cdot \mathbf{n} \, dS \) remains constant at any radial distance from the source

(D) \( \iiint_{S} \mathbf{Re}(\mathbf{P}) \cdot \mathbf{n} \, dS \) decreases with increasing radial distance from the source

Answer: - (D)

Exp: - \( \iiint_{S} \mathbf{Re}(\mathbf{P}) \cdot \mathbf{n} \, dS \) gives average power and it decreases with increasing radial distance from the source.

2. A transmission line of characteristic impedance 50\( \Omega \) is terminated by a 50\( \Omega \) load. When excited by a sinusoidal voltage source at 10GHz, the phase difference between two points spaced 2mm apart on the line is found to be \( \frac{\pi}{4} \) radians. The phase velocity of the wave along the line is

(A) 0.8 \times 10^8 m/s  
(B) 1.2 \times 10^8 m/s  
(C) 1.6 \times 10^8 m/s  
(D) 3 \times 10^8 m/s

Answer: - (C)

Exp: - \( Z_o = 50\Omega \); \( Z_L = 50\Omega \)

For \( \frac{\pi}{4} \) radians the distance is 2mm

The phase velocity \( v_p = \frac{\omega}{\beta} = \frac{2 \times \pi \times 10^{10}}{2\pi} = 16 \times 10^{-3} = 1.6 \times 10^8 m/s \)

3. An analog signal is band-limited to 4kHz, sampled at the Nyquist rate and the samples are quantized into 4 levels. The quantized levels are assumed to be independent and equally probable. If we transmit two quantized samples per second, the information rate is ________ bits / second.

(A) 1  
(B) 2  
(C) 3  
(D) 4

Answer: - (D)

Exp: - Since two samples are transmitted and each sample has 2 bits of information, then the information rate is 4 bits/sec.
4. The root locus plot for a system is given below. The open loop transfer function corresponding to this plot is given by

(A) \( G(s)H(s) = k \frac{s(s + 1)}{(s + 2)(s + 3)} \)

(B) \( G(s)H(s) = k \frac{(s + 1)}{s(s + 2)(s + 3)} \)

(C) \( G(s)H(s) = k \frac{1}{s(s - 1)(s + 2)(s + 3)} \)

(D) \( G(s)H(s) = k \frac{(s + 1)}{s(s + 2)(s + 3)} \)

Answer: - (B)

Exp: - 'x' → indicates pole
'O' → indicates zero
The point on the root locus when the number of poles and zeroes on the real axis to the right side of that point must be odd

5. A system is defined by its impulse response \( h(n) = 2^nu(n-2) \). The system is

(A) stable and causal
(B) causal but not stable
(C) stable but not causal
(D) unstable and non-causal

Answer: - (B)

Exp: - \( h(n) = 2^nu(n-2) \)
\( h(n) \) is existing for \( n>2 \); so that \( h(n) = 0; n < 0 \) ⇒ causal
\[ \sum_{n=-\infty}^{\infty} h(n) = \sum_{n=-\infty}^{\infty} 2^nu(n-2) = \sum_{n=-2}^{\infty} 2^n = \infty \] ⇒ System is unstable

6. If the unit step response of a network is \( 1 - e^{-\alpha t} \), then its unit impulse response is

(A) \( \alpha e^{-\alpha t} \)

(B) \( \alpha^{-1}e^{-\alpha t} \)

(C) \( 1 - \alpha^{-1} e^{-\alpha t} \)

(D) \( 1 - \alpha e^{-\alpha t} \)

Answer: - (A)

Exp: - \( S(t) \) → step response

Impulse response \( h(t) = \frac{d}{dt}(S(t)) = \frac{d}{dt}(1 - e^{-\alpha t}) = \alpha e^{-\alpha t} \)

7. The output \( Y \) in the circuit below is always ‘1’ when
(A) two or more of the inputs P,Q,R are ‘0’
(B) two or more of the inputs P,Q,R are ‘1’
(C) any odd number of the inputs P,Q,R is ‘0’
(D) any odd number of the inputs P,Q,R is ‘1’

Answer: - (B)

Exp: - The output Y expression in the Ckt

\[ Y = PQ + PR + RQ \]

So that two or more inputs are ‘1’, Y is always ‘1’.

8. In the circuit shown below, capacitors \( C_1 \) and \( C_2 \) are very large and are shorts at the input frequency. \( v_i \) is a small signal input. The gain magnitude \( \frac{v_o}{v_i} \) at 10M rad/s is

(A) maximum (B) minimum (C) unity (D) zero

Answer: - (A)

Exp: - In the parallel RLC Ckt

\[ L = 10 \mu H \quad \text{and} \quad C = 1nF \]

\[ \omega_g = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{10 \times 10^{-6} \times 10^{-9}}} = 10^7 \text{rad/s} = 10 \text{Mrad/s} \]

So that for a tuned amplifier, gain is maximum at resonant frequency

9. Drift current in the semiconductors depends upon

(A) only the electric field
(B) only the carrier concentration gradient
(C) both the electric field and the carrier concentration
(D) both the electric field and the carrier concentration gradient

Answer: - (C)

Exp: - Drift current, \( J = \sigma E \)

\[ J = (\eta n_p + p\mu_p)qE \]

So that it depends on carrier concentration and electric field.
10. A Zener diode, when used in voltage stabilization circuits, is biased in
(A) reverse bias region below the breakdown voltage
(B) reverse breakdown region
(C) forward bias region
(D) forward bias constant current mode

Answer: - (B)

Exp: -

For Zener diode
Voltage remains constant in break down region and current carrying capacity in high.

11. The circuit shown below is driven by a sinusoidal input \( v_i = V_p \cos(t/RC) \). The steady state output \( v_o \) is

(A) \( (V_p / 3) \cos(t/RC) \)
(B) \( (V_p / 3) \sin(t/RC) \)
(C) \( (V_p / 2) \cos(t/RC) \)
(D) \( (V_p / 2) \sin(t/RC) \)

Answer: - (A)

Exp: -

\[
\frac{v_o}{v_i} = \frac{z_2}{z_1 + z_2} \quad \text{where} \quad z_2 = R \left| \frac{1}{j\omega C} \right| \quad \text{and} \quad z_1 = R + \frac{1}{j\omega C}
\]

\[
z_2 = \frac{R}{R(j\omega) + 1}
\]

Given \( w = \frac{1}{RC} \) \( \therefore v_i = V_p \cos \left( \frac{t}{RC} \right) \) \( \Rightarrow z_2 = \frac{R}{1+j} \)

\[
z_1 = R + \frac{1}{j\omega C} = R + \frac{1}{jR} \Rightarrow R(1-j)
\]

\[
\frac{v_o}{v_i} = \frac{R}{1+j + R(1-j)} = \frac{1}{1+2} = \frac{1}{3}
\]
12. Consider a closed surface $S$ surrounding volume $V$. If $\vec{r}$ is the position vector of a point inside $S$, with $\hat{n}$ the unit normal on $S$, the value of the integral $\int_S \vec{r} \cdot \hat{n} dS$ is

(A) 3V \hspace{1cm} (B) 5V \hspace{1cm} (C) 10V \hspace{1cm} (D) 15V

Answer: - (D)

Exp: - Apply the divergence theorem

$$\int_S \vec{r} \cdot \hat{n} dS = \int_V \nabla \cdot \vec{r} dV = \int_V 3 dV = 15V \hspace{1cm} (\because \nabla \cdot \vec{r} = 3 \hspace{0.5cm} \text{and} \hspace{0.5cm} \vec{r} \text{ is the position vector})$$

13. The modes in a rectangular waveguide are denoted by $\frac{TE_{mn}}{TM_{mn}}$ where $m$ and $n$ are the eigen numbers along the larger and smaller dimensions of the waveguide respectively. Which one of the following statements is TRUE?

(A) The $TM_{10}$ mode of the wave does not exist

(B) The $TE_{10}$ mode of the wave does not exist

(C) The $TM_{10}$ and the $TE_{10}$ modes both exist and have the same cut-off frequencies

(D) The $TM_{10}$ and $TM_{01}$ modes both exist and have the same cut-off frequencies

Answer: - (A)

Exp: - $TM_{10}$ mode doesn’t exist in rectangular waveguide.

14. The solution of the differential equation $\frac{dy}{dx} = ky$, $y(0) = C$ is

(A) $x = ce^{-ky}$ \hspace{1cm} (B) $x = ke^{xy}$ \hspace{1cm} (C) $y = ke^{x}$ \hspace{1cm} (D) $y = ce^{-ky}$

Answer: - (C)

Exp: - Given $y(0) = C$ and $\frac{dy}{dx} = ky$, $\Rightarrow \frac{dy}{y} = kdx$

$\ln y = kx + C \Rightarrow y = e^{kx} e^{c}$

When $y(0) = C$, $y = k_1 e^{0} \hspace{0.5cm} \therefore y = c e^{kx} \hspace{1cm} (\because k_1 = C)$

15. The Column-I lists the attributes and the Column-II lists the modulation systems. Match the attribute to the modulation system that best meets it

<table>
<thead>
<tr>
<th>Column-I</th>
<th>Column-II</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td>Power efficient transmission of signals</td>
</tr>
<tr>
<td>Q</td>
<td>Most bandwidth efficient transmission of voice signals</td>
</tr>
<tr>
<td>R</td>
<td>Simplest receiver structure</td>
</tr>
<tr>
<td>S</td>
<td>Bandwidth efficient transmission of signals with Significant dc component</td>
</tr>
</tbody>
</table>

(A) P-4; Q-2; R-1; S-3 \hspace{1cm} (B) P-2; Q-4; R-1; S-3

(C) P-3; Q-2; R-1; S-4 \hspace{1cm} (D) P-2; Q-4; R-3; S-1
16. The differential equation \( 100 \frac{d^2y}{dt^2} - 20 \frac{dy}{dt} + y = x(t) \) describes a system with an input \( x(t) \) and an output \( y(t) \). The system, which is initially relaxed, is excited by a unit step input. The output \( y(t) \) can be represented by the waveform.

\[
\frac{d^2y}{dt^2} + 20 \frac{dy}{dt} + y = x(t)
\]

Apply L.T both sides

\[
(s^2 + 20s + 1)Y(s) = \frac{1}{s}
\]

\[
Y(s) = \frac{1}{s(s^2 + 20s + 1)}
\]

So we have poles with positive real part \( \Rightarrow \) system is unstable.
17. For the transfer function $G(j\omega) = 5 + j\omega$, the corresponding Nyquist plot for positive frequency has the form

![Nyquist plots]

(A) \hspace{2cm} (B) \hspace{2cm} (C) \hspace{2cm} (D)

Answer: - (A)
Exp: - As we increases real part ‘5’ is fixed only imaginary part increases.

18. The trigonometric Fourier series of an even function does not have the
(A) dc term  \hspace{1cm} (B) cosine terms  \hspace{1cm} (C) sine terms  \hspace{1cm} (D) odd harmonic terms

Answer: - (C)
Exp: - $f(t)$ is even function, hence $b_k = 0$
Where ‘$b_k$’ is the coefficient of sine terms

19. When the output $Y$ in the circuit below is ‘1’, it implies that data has

![Circuit diagram]

(A) changed from 0 to 1  \hspace{2cm} (B) changed from 1 to 0  \hspace{2cm} (C) changed in either direction  \hspace{2cm} (D) not changed

Answer: - (A)
Exp: - When data is ‘0’, $Q$ is ‘0’
And $Q$ is ‘1’ first flip flop
Data is changed to 1
$Q$ is $1 \rightarrow$ first ‘D’
$Q$’ is connected to 2$^{nd}$ flip flop
So that $Q_2 = 1$
So that the inputs of AND gate is ‘1’ $\Rightarrow Y = '1'$
20. The logic function implemented by the circuit below is (ground implies logic 0)

\[ F = \text{XOR} (P, Q) \]

Answer: - (D)

Exp: - From the CKT

O is connected to 'I_o' & 'I_3'
And '1' is connected to I_1 & I_2
\[ \therefore F = PQ + \overline{PQ} = \text{XOR} (P, Q) \]

21. The circuit below implements a filter between the input current i_i and the output voltage v_o. Assume that the opamp is ideal. The filter implemented is a

\[ (A) \text{ low pass filter} \quad (B) \text{ band pass filter} \]
\[ (C) \text{ band stop filter} \quad (D) \text{ high pass filter} \]

Answer: - (D)

Exp: - When W=0; inductor acts as a S.C \( \Rightarrow v_o = 0 \)

And when \( \omega = \infty \), inductor acts as a O.C \( \Rightarrow v_o = i_1R_1 \)

So it acts as a high pass filter.

22. A silicon PN junction is forward biased with a constant current at room temperature. When the temperature is increased by 10°C, the forward bias voltage across the PN junction

\[ (A) \text{ increases by 60mV} \quad (B) \text{ decreases by 60mV} \]
\[ (C) \text{ increases by 25mV} \quad (D) \text{ decreases by 25mV} \]

Answer: - (D)

Exp: - For Si forward bias voltage change by \(-2.5\text{mv/}^0\text{C}\)

For \(10^0\text{C}\) increases, change will be \(-2.5\times10 = -25\text{mV}\)
23. In the circuit shown below, the Norton equivalent current in amperes with respect to the terminals P and Q is

\[ I = 6.4 - j4.8 \]  

(A) 6.4 – j4.8  
(B) 6.56 – j7.87  
(C) 10 + j0  
(D) 16 + j0

Answer: - (A)

Exp: - When terminals P & Q are S.C
 Then the CKT becomes

24. In the circuit shown below, the value of \( R_L \) such that the power transferred to \( R_L \) is maximum is

(A) 5\( \Omega \)  
(B) 10\( \Omega \)  
(C) 15\( \Omega \)  
(D) 20\( \Omega \)

Answer: - (C)

Exp: - For maximum power transmission \( R_L = R_{th}^* \)

For the calculation of \( R_{th} \)
25. The value of the integral \( \int_{c} \frac{-3z + 4}{z^2 + 4z + 5} \, dz \) where \( c \) is the circle \(|z| = 1\) is given by

(A) 0 (B) 1/10 (C) 4/5 (D) 1

Answer: (A)

Exp: \(- \int_{c} \frac{-3z + 4}{z^2 + 4z + 5} \, dz = 0\)

\( z = -2 \pm j \) will be outside the unit circle

So that integration value is 'zero'.

Q. No. 26 – 51 Carry Two Marks Each

26. A current sheet \( \mathbf{J} = 10 \, \mu A/m \) lies on the dielectric interface \( x=0 \) between two dielectric media with \( \varepsilon_{r1} = 5, \mu_{r1} = 1 \) in Region -1 \((x<0)\) and \( \varepsilon_{r2} = 5, \mu_{r2} = 2 \) in Region -2 \((x>0)\). If the magnetic field in Region-1 at \( x=0^- \) is \( \mathbf{H}_1 = 3\hat{u}_x + 30\hat{u}_y \, A/m \) the magnetic field in Region-2 at \( x=0^+ \) is

\( \mathbf{H}_2 = 1.5\hat{u}_x + 40\hat{u}_y \, A/m \) or \( \mathbf{H}_2 = 1.5\hat{u}_x + 30\hat{u}_y - 10\hat{u}_z \, A/m \)

Answer: (A)

Exp: \( \mathbf{H}_2 = \mathbf{H}_1 \times \mathbf{n} \Rightarrow \mathbf{H}_2 = \mathbf{H}_1 - 10\hat{u}_z = 30\hat{u}_y - 10\hat{u}_z \)

And \( \mathbf{B}_n = \mathbf{B}_2 \)

\( \mu_1 \mathbf{H}_2 = \mu_2 \mathbf{H}_2 \Rightarrow \mathbf{H}_2 = \frac{\mu_1}{\mu_2} \mathbf{H}_2 \)

Normal component in x direction

\( \mathbf{H}_2 = \frac{1}{2} (3) \hat{u}_x = 1.5\hat{u}_x ; \mathbf{H}_2 = 1.5\hat{u}_x + 30\hat{u}_y - 10\hat{u}_z \, A/m \)
27. A transmission line of characteristic impedance 50Ω is terminated in a load impedance \( Z_L \). The VSWR of the line is measured as 5 and the first of the voltage maxima in the line is observed at a distance of \( \frac{\lambda}{4} \) from the load. The value of \( Z_L \) is

(A) 10Ω  
(B) 250Ω  
(C) (19.23 + j46.15)Ω  
(D) (19.23 – j46.15)Ω

Answer: - (A)

Exp: Voltage maximum in the line is observed exactly at \( \frac{\lambda}{4} \)

Therefore '\( z_L \)' should be real

\[
\text{VSWR} = \frac{z_L}{2Z_0} \Rightarrow z_L = \frac{50}{5} = 10Ω \quad (\because \text{Voltage minimum at load})
\]

28. \( X(t) \) is a stationary random process with autocorrelation function \( R_x(\tau) = \exp(\pi \tau^2) \). This process is passed through the system shown below. The power spectral density of the output process \( Y(t) \) is

(A) \((4\pi^2f^2 + 1) \exp(-\pi f^2)\)  
(B) \((4\pi^2f^2 - 1) \exp(-\pi f^2)\)  
(C) \((4\pi^2f^2 + 1) \exp(-\pi f)\)  
(D) \((4\pi^2f^2 - 1) \exp(-\pi f)\)

Answer: - (A)

Exp: The total transfer function \( H(f) = (j2\pi f - 1) \)

\[
S_x(f) = |H(f)|^2 S_x(f)\quad R_x(\tau) \leftrightarrow S_x(f)
\]

\[
= (4\pi^2f^2 + 1)e^{-\pi f^2} \quad (\because e^{-\pi f^2} \leftrightarrow e^{\pi f^2})
\]

29. The output of a 3-stage Johnson (twisted ring) counter is fed to a digital-to-analog (D/A) converter as shown in the figure below. Assume all the states of the counter to be unset initially. The waveform which represents the D/A converter output \( V_o \) is
30. Two D flip-flops are connected as a synchronous counter that goes through the following \( Q_B Q_A \) sequence \( 00 \rightarrow 11 \rightarrow 01 \rightarrow 10 \rightarrow 00 \rightarrow \ldots \)

The combination to the inputs \( D_A \) and \( D_B \) are

(A) \( D_A = Q_B^1, D_B = Q_A^1 \)  
(B) \( D_A = \overline{Q_A^1}, D_B = \overline{Q_B^1} \)  
(C) \( D_A = (Q_A^1 \overline{Q_B^1} + \overline{Q_A^1} Q_B^1); D_B = \overline{Q_A^1} \)  
(D) \( D_A = (Q_A^1 Q_B^1 + \overline{Q_A^1} Q_B^1); D_B = \overline{Q_A^1} \)

Answer: - (D)

Exp: - Q (present) \( Q \) (next)

\[
\begin{array}{cccc}
Q_B & Q_A & Q_B^1 & Q_A^1 \\
0 & 0 & 1 & 1 \\
1 & 1 & 0 & 1 \\
0 & 1 & 1 & 0 \\
1 & 0 & 0 & 0 \\
\end{array}
\]

\[
D_A = \begin{cases} 
\overline{Q_B} & Q_A = 0 \\
Q_B & Q_A = 1 
\end{cases}
\]  

\[
D_B = \begin{cases} 
\overline{Q_A} & Q_B = 0 \\
Q_A & Q_B = 1 
\end{cases}
\]
31. In the circuit shown below, for the MOS transistors, $\mu_n C_{ox} = 100\mu A/V^2$ and the threshold voltage $V_T = 1V$. The voltage $V_x$ at the source of the upper transistor is

(A) 1V  (B) 2V  (C) 3V  (D) 3.67V

Answer: - (C)

Exp: - The transistor which has $\frac{W}{L} = 4$

$V_{DS} = 6 - V_x$ and $V_{GS} = 5 - V_x$

$V_{GS} - V_T = 5 - V_x - 1 = 4 - V_x$

$V_{DS} > V_{GS} - V_T$

So that transistor in saturation region.

The transistor which has $\frac{W}{L} = 1$

Drain is connected to gate

So that transistor in saturation

$V_{DS} > V_{GS} > V_T \quad (\therefore V_{DS} = V_{GS})$

The current flow in both the transistor is same

$$\mu_n C_{ox} \left( \frac{W}{L} \right)_1 \left( \frac{V_{GS}_1}{2} - \frac{V_T}{2} \right)^2 = \mu_n C_{ox} \left( \frac{W}{L} \right)_2 \left( \frac{V_{GS}_2 - V_T}{2} \right)^2$$

$$4 \left( \frac{5 - V_x - 1}{2} \right)^2 = 1 \left( \frac{V_x - 4}{2} \right)^2 \quad (\therefore V_{GS} = V_x - 0)$$

$$4 \left( V_x^2 - 8V_x + 16 \right) = V_x^2 - 2V_x + 1 \Rightarrow 3V_x^2 - 30V_x + 63 = 0 \Rightarrow V_x = 3V$$

32. An input $x(t) = \exp(-2t)u(t) + \delta(t - 6)$ is applied to an LTI system with impulse response $h(t) = u(t)$. The output is is

(A) $[1 - \exp(-2t)]u(t) + u(t + 6)$  (B) $[1 - \exp(-2t)]u(t) + u(t - 6)$

(C) $0.5[1 - \exp(-2t)]u(t) + u(t + 6)$  (D) $0.5[1 - \exp(-2t)]u(t) + u(t - 6)$
33. For a BJT the common base current gain $\alpha = 0.98$ and the collector base junction reverse bias saturation current $I_{C0} = 0.6 \mu A$. This BJT is connected in the common emitter mode and operated in the active region with a base drive current $I_B = 20 \mu A$. The collector current $I_C$ for this mode of operation is
(A) 0.98mA    (B) 0.99mA    (C) 1.0mA    (D) 1.01mA

Answer: - (D)

Exp: $I_C = \beta I_B + (1 + \beta) I_{CBO} = \beta \frac{\alpha}{1 - \alpha} = \frac{0.98}{1 - 0.98} = 49$

$I_B = 20 \mu A, I_{CBO} = 0.6 \mu A \therefore I_C = 1.01mA$

34. If $\mathcal{L}[f(t)] = \frac{2(s+1)}{s^2 + 4s + 7}$ then the initial and final values of $f(t)$ are respectively
(A) 0, 2    (B) 2, 0    (C) 0, 2/7    (D) 2/7, 0

Answer: - (B)

Exp: $\mathcal{L}f(t) = \mathcal{L}\frac{s(2s+1)}{s^2 + 4s + 7}$

\[ \mathcal{L}\left[ \frac{s}{s^2 + 4s + 7} \right] = \frac{2}{7} \]

\[ \mathcal{L}\left[ \frac{s(2s+1)}{s^2 + 4s + 7} \right] = \frac{2s+1}{s^2 + 4s + 7} = 0 \]

35. In the circuit shown below, the current $I$ is equal to

(A) 14\|0^0A    (B) 2.0\|0^0A    (C) 2.8\|0^0A    (D) 3.2\|0^0A

Answer: - (B)

Exp: - Apply the delta – to – star conversion

The circuit becomes
The net Impedance = \((2 + j4) \parallel (2 - j4) + 2 = \frac{4 + 16}{4} + 2 = 7\Omega\)

\[I = \frac{14\angle 0^0}{7} = 2\angle 0^0\text{A}\]

36. A numerical solution of the equation \(f(x) = x + \sqrt{x - 3} = 0\) can be obtained using Newton-Raphson method. If the starting value is \(x = 2\) for the iteration, the value of \(x\) that is to be used in the next step is

(A) 0.306  (B) 0.739  (C) 1.694  (D) 2.306

Answer: - (C)

Exp: -

\[x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}\]

\[f(2) = (2 + \sqrt{2} - 3) = \sqrt{2} - 1\text{ and } f'(2) = 1 + \frac{1}{2\sqrt{2}} = \frac{2\sqrt{2} + 1}{2\sqrt{2}}\]

\[\Rightarrow x_{n+1} = 2 - \frac{(\sqrt{2} - 1)}{x\sqrt{2} + 1} = 1.694\]

37. The electric and magnetic fields for a TEM wave of frequency 14 GHz in a homogeneous medium of relative permittivity \(\varepsilon\), and relative permeability \(\mu = 1\) are given by

\[\mathbf{E} = E_p e^{j(\omega t - 280\pi y)} \hat{\mathbf{u}}_x \text{V/m} \quad \mathbf{H} = 3e^{j(\omega t - 280\pi y)} \hat{\mathbf{u}}_x \text{A/m}\]

Assuming the speed of light in free space to be \(3 \times 10^8\) m/s, the intrinsic impedance of free space to be \(120\pi\), the relative permittivity \(\varepsilon_r\) of the medium and the electric field amplitude \(E_p\) are

(A) \(\varepsilon_r = 3, E_p = 120\pi\)  (B) \(\varepsilon_r = 3, E_p = 360\pi\)

(C) \(\varepsilon_r = 9, E_p = 360\pi\)  (D) \(\varepsilon_r = 9, E_p = 120\pi\)

Answer: - (D)

Exp: -

\[\frac{E}{H} = \eta = \sqrt{\frac{\mu}{\varepsilon}} = 120\pi \sqrt{\frac{\mu_r}{\varepsilon_r}}\]

\[\frac{E_p}{3} = \eta = 120\pi \sqrt{\frac{\mu_r}{\varepsilon_r}}\]

Only option ‘D’ satisfies
38. A message signal \( m(t) = \cos 200\pi t + 4\cos \pi t \) modulates the carrier \( c(t) = \cos 2\pi f_c t \) where \( f_c = 1 \text{ MHZ} \) to produce an AM signal. For demodulating the generated AM signal using an envelope detector, the time constant \( RC \) of the detector circuit should satisfy

(A) \( 0.5 \text{ ms} < RC < 1 \text{ ms} \)  
(B) \( 1\mu\text{s} << RC < 0.5 \text{ ms} \)  
(C) \( RC << \mu\text{s} \)  
(D) \( RC >> 0.5 \text{ ms} \)

Answer: - (B)

Exp: - Time constant should be length than \( \frac{1}{f_m} \)

And time constant should be far greater than \( \frac{1}{f_c} \)

\[
f_m = \frac{4000a}{2a} = 2000
\]

\[
\frac{1}{f_c} << RC < \frac{1}{2000}
\]

\( 1\mu\text{s} << RC << 0.5\text{ms} \)

39. The block diagram of a system with one input \( it \) and two outputs \( y_1 \) and \( y_2 \) is given below.

![Block Diagram](image)

A state space model of the above system in terms of the state vector \( \mathbf{x} \) and the output vector \( \mathbf{y} = [y_1 \ y_2] \) is

(A) \( \dot{\mathbf{x}} = [2] \mathbf{x} + [1] u; \quad \mathbf{y} = [1 \ 2] \mathbf{x} \)

(B) \( \dot{\mathbf{x}} = [-2] \mathbf{x} + [1] u; \quad \mathbf{y} = [1 \ 2] \mathbf{x} \)

(C) \( \dot{\mathbf{x}} = [-2 \ 0 \ 1] \mathbf{x} + [1] u; \quad \mathbf{y} = [1 \ 2] \mathbf{x} \)

(D) \( \dot{\mathbf{x}} = [2 \ 0 \ 1] \mathbf{x} + [1] u; \quad \mathbf{y} = [1 \ 2] \mathbf{x} \)

Answer: - (B)

Exp: - Draw the signal flow graph
From the graph
\[ x = -2x + 4 \; \& \; y_1 = x; \; y_2 = 2x \]
\[ x = \begin{bmatrix} -2 \\ 1 \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \end{bmatrix} \; \begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \end{bmatrix} x \]

40. Two systems \( H_1(z) \) and \( H_2(z) \) are connected in cascade as shown below. The overall output \( y(n) \) is the same as the input \( x(n) \) with a one unit delay. The transfer function of the second system \( H_2(z) \) is

(A) \( \frac{1 - 0.6z^{-1}}{z^{-1}(1 - 0.4z^{-1})} \)
(B) \( \frac{z^{-1} - 0.6z^{-1}}{1 - 0.4z^{-1}} \)
(C) \( \frac{z^{-1}(1 - 0.4z^{-1})}{1 - 0.6z^{-1}} \)
(D) \( \frac{z^{-1}}{1 - 0.6z^{-1}} \)

Answer: - (B)

Exp: - The overall transfer function = \( z^{-1} \) (\( \because \) unit day T.F = \( z^{-1} \))

\( H_1(z)H_2(z) = z^{-1} \); \( H_2(z) = \frac{z^{-1} - 0.6z^{-1}}{1 - 0.4z^{-1}} \)

41. An 8085 assembly language program is given below. Assume that the carry flag is initially unset. The content of the accumulator after the execution of the program is

|MVI A,07H |
| RLC |
| MOV B,A |
| RLC |
| ADD B |
| RRC |

(A) 8CH  (B) 64H  (C) 23H  (D) 15H
Answer: - (C)
Exp: - MVI A, 07 H ⇒ 0000 0111 ← The content of ‘A’
RLC ⇒ 0000 1110 ← The content of ‘A’
MOV B, A ⇒ 0000 1110 ← The content of ‘B’
RLC ⇒ 0001 1100 ← The content of ‘B’
RLC ⇒ 0011 1000 ← The content of ‘B’
ADD B

\[
\begin{array}{c}
A \\
\hline
0000 \\
1110 \\
\hline
B \\
0011 \\
1000 \\
\hline
0100 \\
0110 \\
\hline
\end{array}
\]

\[
\text{RRC } \frac{0010}{2} \text{ and } \frac{0011}{3} \text{ 23H}
\]

42. The first six points of the 8-point DFT of a real valued sequence are 5, 1 – j3, 0, 3 – j4, 0 and 3 + j4. The last two points of the DFT are respectively
(A) 0, 1-j3 
(B) 0, 1+j3 
(C) 1+j3, 5 
(D) 1 – j3, 5

Answer: - (C)
Exp: - DFT points are complex conjugates of each other and they one symmetric to the middle point.
\[
x(0) = x^*(7) \\
x(1) = x^*(6) \\
x(2) = x^*(5) \\
x(3) = x^*(4)
\]

⇒ Last two points will be \(x^*(0)\) and \(x^*(1) = 1 + j3\) and 5

43. For the BJT Q\(_L\) in the circuit shown below, \(\beta = \infty\), \(V_{BE on} = 0.7V\), \(V_{CBE} = 0.7V\). The switch is initially closed. At time \(t = 0\), the switch is opened. The time \(t\) at which \(Q_1\) leaves the active region is

(A) 10 ms  
(B) 25 ms  
(C) 50 ms  
(D) 100 ms

© All rights reserved by Gateforum Educational Services Pvt. Ltd. No part of this document may be reproduced or utilized in any form without the written permission. Discuss GATE 2011 question paper at www.gatementor.com.
Answer: - (C)

Exp: - Apply KVL at the BE junction

\[ I_E = \frac{-5 - 0.7 + 10}{4.3k\Omega} = \frac{-4.3}{4.3k\Omega} = 1mA \]

Always \( I_E = 1mA \); At collector junction

\[ I_{Cap} + (0.5mA) = 1mA \quad (\because \beta = \infty; I_E = I_C) \]

\[ I_{Cap} = 1 - 0.5 = 0.5mA \quad \text{always constant} \]

\( V_{CE} = V_C - V_E \Rightarrow V_C = V_{CE} + V_E \)

\[ V_C = 5V = V_{cap} \]

\[ V_{cap} = I_{Cap} \times \frac{t}{C} \quad \text{Or} \quad t = \frac{V_{cap} (C)}{I_{Cap}} = \frac{(5) \times 5 \times 10^{-6}}{0.5 \times 10^{-3}} = 50ms \]

44. In the circuit shown below, the network \( N \) is described by the following \( Y \) matrix:

\[
Y = \begin{bmatrix}
0.1S & -0.01S \\
0.01S & 0.1S
\end{bmatrix}
\]

the voltage gain \( \frac{V_2}{V_1} \) is

\( (A) \frac{1}{90} \quad (B) -\frac{1}{90} \quad (C) -\frac{1}{99} \quad (D) -\frac{1}{11} \)

Answer: - (D)

Exp: - \( N_1 = 100V + 25I_1 \); \( V_2 = -100I_2 \)

\[ I_2 = Y_3V_1 + Y_4V_2 \Rightarrow -0.01V_2 = 0.01V_1 + 0.1V_2 \Rightarrow \frac{V_2}{V_1} = -\frac{1}{11} \]

45. In the circuit shown below, the initial charge on the capacitor is 2.5 mC, with the voltage polarity as indicated. The switch is closed at time \( t=0 \). The current \( i(t) \) at a time \( t \) after the switch is closed is

\( (A) i(t) = 15 \exp(-2 \times 10^3 t) A \)

\( (B) i(t) = 5 \exp(-2 \times 10^3 t) A \)

\( (C) i(t) = 10 \exp(-2 \times 10^3 t) A \)

\( (D) i(t) = -5 \exp(-2 \times 10^3 t) A \)
Answer: - (A)

Exp: - \[ Q = 2.5\text{mC} \]

\[ V_{\text{initial}} = \frac{2.5 \times 10^{-3} \text{C}}{50 \times 10^{-6} \text{F}} = 50 \text{V} \Rightarrow \text{Thus net voltage} = 100 + 50 = 150 \text{V} \]

\[ i(t) = \frac{150}{10} \exp(-2 \times 10^3 t) \text{A} = 15 \exp(-2 \times 10^3 t) \text{A} \]

46. The system of equations

\[ x + y + z = 6 \]
\[ x + 4y + 6z = 20 \]
\[ x + 4y + \lambda z = \mu \]

has NO solution for values of \( \lambda \) and \( \mu \) given by

(A) \( \lambda = 6, \mu = 20 \)  (B) \( \lambda = 6, \mu \neq 20 \)  (C) \( \lambda \neq 6, \mu = 20 \)  (D) \( \lambda \neq 6, \mu \neq 20 \)

Answer: - (B)

Exp: - Given equations are

\[ x + y + z = 6, x + 4y + 6z = 20 \text{ and } x + 4y + \lambda z = \mu \]

If \( \lambda = 6 \) and \( \mu = 20 \), then \( x + 4y + 6z = 20 \)

Infinite solution

If \( \lambda = 6 \) and \( \mu \neq 20 \), then

\[ x + 4y + 6z = 20, x + 4y + 6z = \mu \]

(\( \mu \neq 20 \)) no solution

If \( \lambda \neq 6 \) and \( \mu = 20 \)

\[ x + 4y + 6z = 20 \]
\[ x + 4y + \lambda z = 20 \]

\[ \lambda \neq 6 \text{ and } \mu \neq 20 \] will also give solution

47. A fair dice is tossed two times. The probability that the second toss results in a value that is higher than the first toss is

(A) \( \frac{2}{36} \)  (B) \( \frac{2}{6} \)  (C) \( \frac{5}{12} \)  (D) \( \frac{1}{2} \)

Answer: - (C)

Exp: - Total number of causes = 36

Total number of favorable causes = \( 5 + 4 + 3 + 2 + 1 = 15 \)

Then probability = \( \frac{15}{36} = \frac{5}{12} \)

\( (1,1) \quad (2,1) \quad (3,1) \quad (4,1) \quad (5,1) \quad (6,1) \)
Common Data Questions: 48 & 49

The channel resistance of an N-channel JFET shown in the figure below is 600 Ω when the full channel thickness (t_{ch}) of 10\,\mu\text{m} is available for conduction. The built-in voltage of the gate P^+ N junction (V_{bi}) is -1 V. When the gate to source voltage (V_{GS}) is 0 V, the channel is depleted by 1\,\mu\text{m} on each side due to the built-in voltage and hence the thickness available for conduction is only 8\,\mu\text{m}

48. The channel resistance when V_{GS} = -3 V is
(A) 360Ω  (B) 917Ω  (C) 1000Ω  (D) 3000Ω
Answer: - (C)

Exp: Width of the depletion large \( W \propto \sqrt{V_{bi} + V_{GS}} \)
\[
\frac{W_2}{W_1} = \sqrt{\frac{-1 - 3}{-1}} \Rightarrow w_2 = 2w_1 = 2(1\,\mu\text{m}) = 2\,\mu\text{m}
\]
So that channel thickness = 10 – 4 = 6\,\mu\text{m}
8\,\mu\text{m} – 750
6\,\mu\text{m} – ?
\[
r_d = \frac{8}{6} \times 750 = 1000 \,\Omega
\]

49. The channel resistance when V_{GS} = 0 V is
(A) 480Ω  (B) 600Ω  (C) 750Ω  (D) 1000Ω

© All rights reserved by Gateforum Educational Services Pvt. Ltd. No part of this document may be reproduced or utilized in any form without the written permission. Discuss GATE 2011 question paper at www.gatementor.com.
Answer: - (C)

Exp: - $r_{don} = \frac{1}{t_{oh}}$

At $V_{GS} = 0$, $t_{ch} = 10 \mu m$; $\text{(Given } r_d = 600 \Omega)$

$r_d = \frac{10}{8} \times 600 \Leftarrow \text{at } 8 \mu m = 750 \Omega$

**Common Data Questions: 50 & 51**

The input-output transfer function of a plant 

$$H(s) = \frac{100}{s(s+10)^2}$$

The plant is placed in a unity negative feedback configuration as shown in the figure below.

50. The gain margin of the system under closed loop unity negative feedback is

(A) 0dB  (B) 20dB  (C) 26 dB  (D) 46 dB

Answer: - (C)

Exp: 

$$H(s) = \frac{100}{s(s+10)^2}$$

Phase cross over frequency = $-90 - 2 \tan^{-1} \left( \frac{\omega}{10} \right) = -180^\circ$

$$\Rightarrow -2 \tan^{-1} \left( \frac{\omega}{10} \right) = -90^\circ \Rightarrow \tan^{-1} \left( \frac{\omega}{10} \right) = 45^\circ \Rightarrow \omega = 10 \text{ rad/ sec}$$

$$\Rightarrow H(j\omega) = \frac{100}{|10(10j+10)|^2} = \frac{1}{10.2} = \frac{1}{20}$$

$$\text{GM} = 20 \log \frac{1}{1/20} = 20 \log 20 = 26 \text{dB}$$

51. The signal flow graph that **DOES NOT** model the plant transfer function $H(s)$ is

- (A) 
- (B) 
- (C) 
- (D)
Answer: - (D)
Exp: -(D) Option (D) does not fix for the given transfer function.

**Linked Answer Questions: Q.52 to Q.55 Carry Two Marks Each**

**Statement for Linked Answer Questions: 52 & 53**

In the circuit shown below, assume that the voltage drop across a forward biased diode is 0.7 V. The thermal voltage \( V_T = kT / q = 25 \text{mV} \). The small signal input \( v_i = V_p \cos(\omega t) \) where \( V_p = 100 \text{mV} \).

![Diagram of the circuit](image)

52. The bias current \( I_{DC} \) through the diodes is

(A) 1 mA
(B) 1.28 mA
(C) 1.5 mA
(D) 2 mA

Answer: - (A)
Exp: \( I_{DC} = \frac{12.7 - (0.7 + 0.7 + 0.7 + 0.7)}{9900} = 1 \text{mA} \)

53. The ac output voltage \( V_{ac} \) is

(A) 0.25 \( \cos(\omega t) \) mV
(B) 1 \( \cos(\omega t) \) mV
(C) 2 \( \cos(\omega t) \) mV
(D) 22 \( \cos(\omega t) \) mV

Answer: - (C)
Exp: - AC dynamic resistance, \( r_d = \eta V_T \frac{I_D}{1 \text{mA}} = \frac{2 \times 25 \text{mV}}{1 \text{mA}} = 50 \Omega \)

\( \eta = 2 \) for Si (\( \therefore \) forward drop = 0.7V)

The ac dynamic resistance offered by each diode = 50 \( \Omega \)

\( \because V_{ac} = V_i (\text{ac}) \left( \frac{4 \times 50 \Omega}{9900 + 50} \right) = 200 \times 10^{-3} \cos \left[ \frac{100}{10000} \right] \)

\( V_{ac} = 2 \cos(\omega t) \) mV
Statement for Linked Answer Questions: 54 & 55

A four-phase and an eight-phase signal constellation are shown in the figure below.

54. For the constraint that the minimum distance between pairs of signal points be \( d \) for both constellations, the radii \( r_1 \) and \( r_2 \) of the circles are

(A) \( r_1 = 0.707d, \ r_2 = 2.782d \)  
(B) \( r_1 = 0.707d, \ r_2 = 1.932d \)  
(C) \( r_1 = 0.707d, \ r_2 = 1.545d \)  
(D) \( r_1 = 0.707d, \ r_2 = 1.307d \)

Answer: - (D)

Exp:-  For 1\textsuperscript{st} constellation

\[ r_1^2 + r_2^2 = d^2 \Rightarrow r_1^2 = d^2 / 2 \Rightarrow r_1 = 0.707d \]

For 2\textsuperscript{nd} constellation

\[ d / 2 = r_2 \cos 67.5 \]

\[ r_2 = 1.307d \]

55. Assuming high SNR and that all signals are equally probable, the additional average transmitted signal energy required by the 8-PSK signal to achieve the same error probability as the 4-PSK signal is

(A) 11.90 dB  
(B) 8.73 dB  
(C) 6.79 dB  
(D) 5.33 dB

Answer: - (D)

Exp:- Energy \( = r_1^2 \) and \( r_2^2 \)  
\[ \frac{r_1^2}{r_2^2} = \left(\frac{0.707d}{1.307d}\right)^2 \]

Energy (in dD) \( = 10 \log \left( \frac{1.307^2}{0.707^2} \right) = 5.33 \text{dB} \)

Q. No. 56 – 60 Carry One Mark Each

56. There are two candidates P and Q in an election. During the campaign, 40% of the voters promised to vote for P, and rest for Q. However, on the day of election 15% of the voters went back on their promise to vote for P and instead voted for Q. 25% of the voters went back on their promise to vote for Q and instead voted for P. Suppose, P lost by 2 votes, then what was the total number of voters?

(A) 100  
(B) 110  
(C) 90  
(D) 95

Answer: - (A)
Exp: - \[
\begin{array}{c|c}
P & Q \\
\hline
40\% & 60\% \\
-6\% & +6\% \\
+15\% & -15\% \\
49\% & 51\% \\
\end{array}
\]

\[
\therefore 2\% = 2 \\
100\% = 100
\]

57. Choose the most appropriate word from the options given below to complete the following sentence:

It was her view that the country’s problems had been_________ by foreign technocrats, so that to invite them to come back would be counter-productive.

(A) Identified  (B) ascertained  (C) Texacerbated  (D) Analysed

Answer: - (C)

Exp: -The clues in the question are ---foreign technocrats did something negatively to the problems – so it is counter-productive to invite them. All other options are non-negative. The best choice is exacerbated which means aggravated or worsened.

58. Choose the word from the options given below that is most nearly opposite in meaning to the given word:

Frequency

(A) periodicity  (B) rarity  (C) gradualness  (D) persistency

Answer: - (B)

Exp: - The best antonym here is rarity which means shortage or scarcity.

59. Choose the most appropriate word from the options given below to complete the following sentence: Under ethical guidelines recently adopted by the Indian Medical Association, human genes are to be manipulated only to correct diseases for which__________ treatments are unsatisfactory.

(A) Similar  (B) Most  (C) Uncommon  (D) Available

Answer: - (D)

Exp: - The context seeks to take a deviation only when the existing/present/current/alternative treatments are unsatisfactory. So the word for the blank should be a close synonym of existing/present/current/alternative. Available is the closest of all.

60. The question below consists of a pair of related words followed by four pairs of words. Select the pair that best expresses the relation in the original pair: Gladiator : Arena

(A) dancer : stage  (B) commuter: train  (C) teacher : classroom  (D) lawyer : courtroom

Answer: - (D)
Exp: - The given relationship is worker: workplace. A gladiator is (i) a person, usually a professional combatant trained to entertain the public by engaging in mortal combat with another person or a wild. (ii) A person engaged in a controversy or debate, especially in public.

Q. No. 61 – 65 Carry Two Marks Each

61 The fuel consumed by a motorcycle during a journey while traveling at various speeds is indicated in the graph below.

The distances covered during four laps of the journey are listed in the table below

<table>
<thead>
<tr>
<th>Lap</th>
<th>Distance (kilometers)</th>
<th>Average speed (kilometers per hour)</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td>15</td>
<td>15</td>
</tr>
<tr>
<td>Q</td>
<td>75</td>
<td>45</td>
</tr>
<tr>
<td>R</td>
<td>40</td>
<td>75</td>
</tr>
<tr>
<td>S</td>
<td>10</td>
<td>10</td>
</tr>
</tbody>
</table>

From the given data, we can conclude that the fuel consumed per kilometre was least during the lap

(A) P  (B) Q  (C) R  (D) S

Answer: - (A)

Exp: -

<table>
<thead>
<tr>
<th>Lap</th>
<th>Fuel consumption (km/l)</th>
<th>Actual fuel consumption</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td>60</td>
<td>$\frac{15}{60} = \frac{1}{4}$</td>
</tr>
<tr>
<td>Q</td>
<td>90</td>
<td>$\frac{75}{90} = \frac{5}{6}$</td>
</tr>
<tr>
<td>R</td>
<td>75</td>
<td>$\frac{40}{75} = \frac{8}{15}$</td>
</tr>
<tr>
<td>S</td>
<td>30</td>
<td>$\frac{10}{30} = \frac{1}{3}$</td>
</tr>
</tbody>
</table>

© All rights reserved by Gateforum Educational Services Pvt. Ltd. No part of this document may be reproduced or utilized in any form without the written permission. Discuss GATE 2011 question paper at www.gatementor.com.
62. Three friends, R, S and T shared toffee from a bowl. R took $\frac{1}{3}$ of the toffees, but returned four to the bowl. S took $\frac{1}{4}$ of what was left but returned three toffees to the bowl. T took half of the remainder but returned two back into the bowl. If the bowl had 17 toffees left, how many toffees were originally there in the bowl?

(A) 38  (B) 31  (C) 48  (D) 41

Answer: - (C)

Exp: - Let the total number of toffees is bowl $x$

R took $\frac{1}{3}$ of toffees and returned 4 to the bowl

$\therefore$ Number of toffees with $R = \frac{1}{3}x - 4$

Remaining of toffees in bowl = $\frac{2}{3}x + 4$

Number of toffees with $S = \frac{1}{4}\left(\frac{2}{3}x + 4\right) - 3$

Remaining toffees in bowl = $\frac{3}{4}\left(\frac{2}{3}x + 4\right) + 4$

Number of toffees with $T = \frac{1}{2}\left[\frac{3}{4}\left(\frac{2}{3}x + 4\right) + 4\right] + 2$

Remaining toffees in bowl = $\frac{1}{2}\left[\frac{3}{4}\left(\frac{2}{3}x + 4\right) + 4\right] + 2$

Given,$\frac{1}{2}\left[\frac{3}{4}\left(\frac{2}{3}x + 4\right) + 4\right] + 2 = 17 \Rightarrow \frac{3}{4}\left(\frac{2}{3}x + 4\right) = 27 \Rightarrow x = 48$

63. Given that $f(y) = |y| / y$, and $q$ is any non-zero real number, the value of $|f(q) - f(-q)|$ is

(A) 0  (B) -1  (C) 1  (D) 2

Answer: - (D)

Exp: - Given, $f(y) = \frac{|y|}{y} \Rightarrow f(q) = \frac{|q|}{q}$ ; $f(-q) = \frac{|-q|}{-q} = \frac{|q|}{q}$

$|f(q) - f(-q)| = \frac{|q|}{q} + \frac{|q|}{q} = \frac{2|q|}{q} = 2$

64. The sum of $n$ terms of the series $4 + 44 + 444 + \ldots$ is

(A) $\frac{4}{81}\left[10^{n-1} - 9n - 1\right]$  (B) $\frac{4}{81}\left[10^{n-1} - 9n - 1\right]$

(C) $\frac{4}{81}\left[10^{n-1} - 9n - 10\right]$  (D) $\frac{4}{81}\left[10^n - 9n - 10\right]$

© All rights reserved by Gateforum Educational Services Pvt. Ltd. No part of this document may be reproduced or utilized in any form without the written permission. Discuss GATE 2011 question paper at www.gatementor.com.
Answer: - (C)

Exp: - Let 
\[
S = 4 \left(1 + 11 + 111 + \ldots\ldots\right) = \frac{4}{9} \left(9 + 99 + 999 + \ldots\ldots\right)
\]
\[
= \frac{4}{9} \left\{ (10 - 1) + (10^2 - 1) + (10^3 - 1) + \ldots\ldots \right\}
\]
\[
= \frac{4}{9} \left\{ (10 + 10^2 + \ldots\ldots10^n) - n \right\} = \frac{4}{9} \left\{ \frac{10^n - 1}{9} - n \right\} = \frac{4}{81} \{10^n - 9n - 10\}
\]

65. The horse has played a little known but very important role in the field of medicine. Horses were injected with toxins of diseases until their blood built up immunities. Then a serum was made from their blood. Serums to fight with diphtheria and tetanus were developed this way.

It can be inferred from the passage that horses were
(A) given immunity to diseases (B) generally quite immune to diseases
(C) given medicines to fight toxins (D) given diphtheria and tetanus serums

Answer: - (B)

Exp: - From the passage it cannot be inferred that horses are given immunity as in (A), since the aim is to develop medicine and in turn immunize humans. (B) is correct since it is given that horses develop immunity after some time. Refer "until their blood built up immunities". Even (C) is invalid since medicine is not built till immunity is developed in the horses. (D) is incorrect since specific examples are cited to illustrate and this cannot capture the essence.