## GENERAL APTITUDE

## Q. No. 1-10 Carry One Mark Each

1. The current population of a city is $11,02,500$. If it has been increasing at the rate of $5 \%$ per annum, what was its population 2 years ago?
(A) 9,92,500
(B) $12,51,506$
(C) 9,95,006
(D) 10,00,000

Key: (D)
Sol: Given,
Current population of a city $=11,02,500$
Increasing rate $=5 \% /$ Annum
The population 2 years ago $=$ ?
Let us assume, the population 2 years ago $=x$
Using compound interest formula, we have

$$
\begin{aligned}
& A=P\left(1+\frac{R}{100}\right)^{n} \\
& \Rightarrow 11,02,500=x\left(1+\frac{5}{100}\right)^{2} \\
& \Rightarrow 11,02,500 \times \frac{100 \times 100}{105 \times 105}=x \\
& \Rightarrow x=10,00,000
\end{aligned}
$$

$\therefore$ The population 2 years ago $=10,00,000$.
2. Given below are two statements and two conclusions.

Statement 1: All purple are green.
Statement 2: All black are green.
Conclusion I: Some black are purple
Conclusion II: No black is purple
Based on the above statements and conclusions, which one of the following options is logically CORRECT?
(A) Either conclusion I or II is correct
(B) Only conclusion I is correct
(C) Both conclusion I and II are correct
(D) Only conclusion II is correct

Key: (A)

Sol:


No black is purple


Some black are purple
3. Computers are ubiquitous. They are used to improve efficiency in almost all fields from agriculture to space exploration. Artificial intelligence (AI) is currently a hot topic. AI enables computers to learn, given enough training data. For humans, sitting in front of a computer for long hours can lead to health issues.

Which of the following can be deduced from the above passage?
(i) Nowadays, computers are present in almost all places.
(ii) Computers cannot be used for solving problems in engineering.
(iii) For humans, there are both positive and negative effects of using computers.
(iv) Artificial intelligence can be done without data.
(A) (ii) and (iv)
(B) (i) and (iii)
(C) (ii) and (iii)
(D) (i), (iii) and (iv)

Key: (B)
4. Consider a square sheet of a side 1 unit. In the first step, it is cut along the main diagonal to get two triangles. In the next step, one of the cut triangles is revolved about its short edge to form a solid cone. The volume of the resulting cone, in cubic units, is $\qquad$ _.
(A) $\frac{\pi}{3}$
(B) $\frac{2 \pi}{3}$
(C) $3 \pi$
(D) $\frac{3 \pi}{2}$

Key: (A)

Sol: Volume of cone $=\frac{\pi}{3} \times r^{2} h=\frac{\pi}{3} \times 1 \times 1=\frac{\pi}{3}$ unit $^{3}$


1


Radius of base circle $=1$ unit
Height of cone $=1$ unit
5. Consider the following sentences:
(i) I woke up from sleep
(ii) I woked up from sleep
(iii) I was woken up from sleep
(iv) I was wokened up from sleep

Which of the above sentences are grammatically CORRECT?
(A) (i) and (iv)
(B) (i) and (iii)
(C) (ii) and (iii)
(D) (i) and (ii)

Key: (B)
6.


Corners are cut from an equilateral triangle to produce a regular convex hexagon as shown in the figure above.

The ratio of the area of the regular convex hexagon to the area of the original equilateral triangle is
(A) $4: 5$
(B) $5: 6$
(C) $3: 4$
(D) $2: 3$

Key: (D)
Sol: In regular hexagon, each interior angle $=120^{\circ}$,
So, if we cut corners of an equilateral triangle, then the removed triangles are also equilateral triangles.
$\therefore \quad$ Let, side of regular hexagon $=\mathrm{x}$ units
Then, side of original equilateral triangle $=3 \mathrm{x}$
$\therefore \quad$ Area of regular hexagon $=\frac{3 \sqrt{3}}{2} \mathrm{x}^{2}$
Area of equilateral triangle $=\frac{\sqrt{3}}{4}(3 x)^{2}$
$\therefore$ Required ratio $=\frac{3 \sqrt{3}}{2} x^{2}: \frac{\sqrt{3}}{4}(3 x)^{2}=\frac{3 \sqrt{3}}{2} x^{2}: \frac{9 \sqrt{3}}{4} x^{2}=1: \frac{3}{2}=2: 3$
7.


The least number of squares that must be added so that the line P-Q becomes the line of symmetry is
$\qquad$ —.
(A) 6
(B) 3
(C) 4
(D) 7

Key: (A)

Sol:

$\therefore \quad$ The least number of squares added $=6$.
8. p and q are positive integers and $\frac{\mathrm{p}}{\mathrm{q}}+\frac{\mathrm{q}}{\mathrm{p}}=3$, then, $\frac{\mathrm{p}^{2}}{\mathrm{q}^{2}}+\frac{\mathrm{q}^{2}}{\mathrm{p}^{2}}=$
(A) 3
(B) 9
(C) 7
(D) 11

Key: (C)
Sol: $\quad$ Given, $\frac{p}{q}+\frac{q}{p}=3$
Squaring on both sides; we get

$$
\left(\frac{p}{q}+\frac{q}{p}\right)^{2}=9 \Rightarrow \frac{p^{2}}{q^{2}}+\frac{q^{2}}{p^{2}}+2=9 \Rightarrow \frac{p^{2}}{q^{2}}+\frac{q^{2}}{p^{2}}=7
$$

9. Nostalgia is to anticipation as $\qquad$ is to $\qquad$
Which one of the following options maintains a similar logical relation in the above sentence?
(A) Future, present
(B) Past, future
(C) Future, past
(D) Present, past

Key: (B)
10.


The number of minutes spent by two students, X and Y , exercising every day in a given week are shown in the bar chart above.

The number of days in the given week in which one of the students spent a minimum of $10 \%$ more than the other student, on a given day, is
(A) 4
(B) 7
(C) 6
(D) 5

Key: (C)
Sol: From the bar graph, it is clear that except Thursday, on all days one of the students spent a minimum of $10 \%$ more than the other student.

## PRODUCTION \& INDUSTRIAL ENGINEERING

## Q. No. 1-25 Carry One Mark Each

1. A product has an exponential time-to-failure distribution with a constant failure rate of 0.00006 per hour. The reliability of the product after 4000 hours of operation is
(A) 0.5866
(B) 0.6866
(C) 0.7866
(D) 0.8866

Key: (C)
2. In a typical product development process under concurrent engineering approach, all elements of product life cycle from conception to disposal are considered at
(A) Product design stage
(B) Process design stage
(C) Manufacturing stage
(D) Disposal stage

Key: (A)
3. When acceptance number of a single sampling plan under attribute category is zero with sample size less than or equal to 10 , the Operating Characteristics (OC) curve is
(A) A horizontal line
(B) A vertical line
(C) A convex function
(D) An inverted S-shaped curve

Key: (C)
4. Which one of the following is an improvement type heuristic algorithm for computerized layout design technique?
(A) Systematic layout planning (SLP)
(B) Computerized relative allocation of facilities technique (CRAFT)
(C) Computerized relationship layout planning (CORELAP)
(D) Plant layout analysis and evaluation technique (PLANET)

Key: (B)
5. Which one of the following is NOT a measure of forecast error?
(A) Mean absolute deviation (MAD)
(B) Mean squared error (MSE)
(C) Mean absolute percent error (MAPE)
(D) Mean sum product error (MSPE)

Key: (D)
6. Pearlie microstructure in an eutectoid steel consists of alternating layers of two phases, namely $\alpha$ ferrite and
(A) Martensite
(B) Austentie
(C) Cementite
(D) Bainite

Key: (C)
7. Which one of the following defects is NOT associated with welding processes?
(A) Angular distortion
(B) Hot tear
(C) Hydrogen embrittlement
(D) Earring

Key: (D)
8. Match the component with the corresponding manufacturing process in the table below.

| Component | Manufacturing process |
| :--- | :--- |
| P. Aluminum alloy piston for IC engine | 1. Blow molding |
| Q. Low carbon steel oil pan | 2. Powder metallurgy |
| R. Tugsten carbide cutting tool insert | 3. Sand casting |
| S. $\quad$ Plastic bottle | 4. $\quad$ Deep drawing |

(A) P-3, Q-2, R-1, S-4
(B) P-3, Q-4, R-2, S-1
(C) P-2, Q-3, R-4, S-1
(D) P-1, Q-3, R-2, S-4

Key: (B)
9. In a turning operation, doubling the cutting speed $(\mathrm{V})$ reduces the tool life ( T ) to $\frac{1}{8^{\text {th }}}$ of the original tool life. The exponent n in the Taylor's tool life equation, $\mathrm{VT}^{\mathrm{n}}=\mathrm{C}$ is
(A) $\frac{1}{2}$
(B) $\frac{1}{3}$
(C) $\frac{1}{4}$
(D) $\frac{1}{8}$

Key: (B)
10. Which one among the following mechanism is NOT used for transforming rotation to translation in machine tools?
(A) Scrw-nut system
(B) 4-bevel gear type differential mechanism
(C) Cam and cam follower system
(D) Whitworth mechanism

Key: (B)
11. Match the Measuring feature with the corresponding Measuring instrument in the table below.

| Measuring feature | Measuring instrument |
| :--- | :--- |
| P. Flatness error of a surface | 1. Auto collimator |
| Q. Profile or a cam | 2. Tool maker's microcope |
| R. . Alignment error of a machine tool slide <br> way | 3. Dividing head and dial gauge |
| S. $\quad$ Pitch and angle error of screw thread | 4. Optical interferometer |

(A) P-4, Q-1, R-2, S-3
(B) P-1, Q-3, R-4, S-2
(C) P-2, Q-4, R-3, S-1
(D) P-4, Q-3, R-1, S-2

Key: (D)
12. The frequency of pulsing in die-sinking electric discharge machine (EDM) is 10 kHz . The pulse off-time is set at 40 micro-seconds. The duty factor at this setting is
(A) 0.40
(B) 0.60
(C) 0.67
(D) 2.50

Key: (B)
13. A cantilever beam of length 0.3 m is subjected to a uniformly distributed load $\mathrm{C}=10 \mathrm{kN} / \mathrm{m}$, as shown in the figure. The bending (flexural) rigidity of the beam is $5000 \mathrm{Nm}^{2}$. Neglecting the self-weight of the beam, the magnitude of beam curvature in $\mathrm{m}^{-1}$ at the fixed end is

(A) 1.10
(B) 0.02
(C) 0.09
(D) 0.05

Key: (C)
14. A circular rod of length $\ell=2 \mathrm{~m}$ is subjected to a compressive load P , as shown in the figure. The bending (flexural) rigidity of the rod is $2000 \mathrm{Nm}^{2}$. If both ends are pinned, then the critical load $\mathrm{P}_{\text {cr }}$ in N (rounded to the nearest integer) at which the rod buckles elastically is

(A) 4935
(B) 2000
(C) 5167
(D) 1238

Key: (A)
15. Two cylindrical parts of equal length $\ell$, as shown in the figure, made of steel having Young's module $\mathrm{E}=200 \mathrm{GPa}$ and Poisson's ratio $\mathrm{v}=0.33$ are press fitted upon one another. If radial interference $\delta=0.05 \mathrm{~mm}$, and radii $\mathrm{R}=25 \mathrm{~mm}$ and $\mathrm{R}_{0}=40 \mathrm{~mm}$, then the contact pressure P in MPa at the interface upon press fit is

(A) 10.7
(B) 60.9
(C) 121.9
(D) 1005.3

Key: (C)
16. The dimensionless number defined by the ratio of inertial force to viscous force is called
(A) Mach number
(B) Froude number
(C) Weber number
(D) Reynolds number

Key: (D)
17. A smallo capillary tube of 3 mm inner diameter is inserted into a fluid having density $900 \mathrm{~kg} / \mathrm{m}^{3}$, surface tension $0.1 \mathrm{~N} / \mathrm{m}$, and contact angle $30^{\circ}$. The rise in the height of fluid in the capillary tube due to surface tension is
(A) 111.4 mm
(B) 128.3 mm
(C) 89.1 mm
(D) 154.1 mm

Key: (B)
18. A given steel has identical yield strength of 700 MPa in unit-axial tension and uni-axial compression. If the steel is subjected to pure shear stress such that the three principal stresses are $\sigma_{1}=\sigma, \sigma_{2}=0, \sigma_{3}=-\sigma$ with $\sigma_{1} \geq \sigma_{2} \geq \sigma_{3}$, then the stress $\sigma$ in MPa for the initiation of plastic yielding in the steel as per von Mises yield criterion is $\qquad$ (round off to 2 decimal places)
Key: (404.1-404.2)
19. A cylindrical mild steel tensile test specimen of gauge length 50 mm and diameter 10 mm is extended in two stages at a deformation speed of $4 \mathrm{~mm} / \mathrm{min}$. The specimen is extended from 50 mm to 55 mm in the first stage, and from 55 mm to 60 mm in the second stage. Neglecting elastic deformation, the total longitudinal trur strain is $\qquad$ . (round off to 2 decimal places).

Key: (0.18)
20. A M30 bolt needs to be subjected to pretention $F_{i}=350 \mathrm{kN}$. If the torque coefficient K of the bolt is 0.2 , then the torque in Nm needed to achieve this pretension is $\qquad$ (in integer).
Key: (2100)
21. A 150 mm wide polyamide flat belt is transmitting 15 kW power through a belt-pulley system. The driving pulley of 150 mm pitch diameter is rotating at 200 RPM. If $F_{1}$ is the belt tension on high tension side, and $F_{2}$ is the belt tension on low tension side, then the difference in belt tensions $\Delta F=F_{1}-F_{2}$ in $N$ is $\qquad$ (round off to one decimal place).
Key: (9549.1-9549.4)
22. Heat is being removed from a refrigerator at a rate of $300 \mathrm{~kJ} / \mathrm{min}$ to maintain its inside temperature at $2^{\circ} \mathrm{C}$. If the input power to the refrigerator is 2 kW , the coefficient of performance of the refrigerator is
$\qquad$ (round off to one decimal place).
Key: (2.5)
23. In an ideal Otto cycle, $800 \mathrm{~kJ} / \mathrm{kg}$ is transferred to air during the constant volume heat addition process and $381 \mathrm{~kJ} / \mathrm{kg}$ is removed during the constant volume heat rejection process. The thermal efficiency in \% of the cycle is $\qquad$ (rounded off to one decimal place).

Key: (52.2-52.5)
24. If $(3 i+1) x+(4 i+4) y+5=0$ with $x$, $y$ being real and $i=\sqrt{-1}$, then $x=$ $\qquad$ (correct up to one decimal place).

Key: (2.5)
25. The minimum value of function $f$ defined by
$f(x, y, z)=x^{2}+5 y^{2}+5 z^{2}-4 x+40 y-40 z+300$
is $\qquad$ (integer)

Key: (136)

## Q. No. 26-55 Carry Two Marks Each

26. For a given process control charge, there are four rules for determinant out-of-control state of the process which are being used simultaneously. The probability of Type-I error for the four rule are 0.005 , $0.02,0.03$, and 0.05 . Assuming independence of the rules, the probability of overall Type-I error when all the four rules are used simultaneously is
(A) 0.101
(B) 0.201
(C) 0.001
(D) 0.301

Key: (A)
27. An in-control process has an estimated standard deviation of 2 mm . The specification limits of the component being processed are $120 \pm 8 \mathrm{~mm}$. When the process mean shifts to 118 mm , the value of the process capability indices, $\mathrm{C}_{\mathrm{p}}$ and $\mathrm{C}_{\mathrm{pk}}$, respectively are,
(A) 1.000, 1.667
(B) 1.333, 1.667
(C) 1.333, 1.000
(D) $1.000,1.000$

Key: (C)
28. There are a number of identical components in a parallel system. When the system reliability is 0.97 and the reliability of each individual component is 0.68 , the number of identical components in the system is (if actual value is a fraction, it may be rounded up to the next higher integer).
(A) 2
(B) 4
(C) 6
(D) 8

Key: (B)
29. A retail chain company has identified four sites $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D to open a new retail store. The company has selected four factors as the basis for evaluation of these sites. The factors, their weights, and the score for each site are given in the following table.

| Factor | Factor weight | Score for site (out of 100) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | A | B | C | D |
| Average community income |  | 60 | 70 | 80 | 50 |
| Demand growth potential | 0.1 | 30 | 80 | 50 | 40 |
| Proximity to existing store | 0.3 | 50 | 10 | 40 | 60 |
| Availability of public transport | 0.2 | 40 | 30 | 40 | 20 |

The site that should be selected to open the new retail store is
(A) Site A
(B) Site B
(C) Site C
(D) Site D

Key: (C)
30. In the classical economic order quantity (EOQ) model, let Q and C denote the optimal order quantity and the corresponding minimum total annual cost (the sum of the inventory holding and ordering costs). If the order quantity is estimated incorrectly as $\mathrm{Q}^{\prime}=2 \mathrm{Q}$, then the corresponding total annual cost $\mathrm{C}^{\prime}$ is
(A) $\mathrm{C}^{\prime}=1.25 \mathrm{C}$
(B) $\mathrm{C}^{\prime}=1.5 \mathrm{C}$
(C) $\mathrm{C}^{\prime}=1.75 \mathrm{C}$
(D) $\mathrm{C}^{\prime}=2 \mathrm{C}$

Key: (A)
31. The eigen values of matrix $A=\left[\begin{array}{ll}8 & 3 \\ 2 & 7\end{array}\right]$ are 5 and 10. For matrix $B=A+\alpha I$, where $\alpha$ is a constant and I is $2 \times 2$ identity matrix, its eigen values are
(A) 5,10
(B) $5+\alpha, 10+\alpha$
(C) $5-\alpha, 10-\alpha$
(D) $5 \alpha, 10 \alpha$

Key: (B)
32. A company manufactures two products P and Q with unit profit of 4 and 5, respectively. The production requires manpower and two kinds of raw materials R1 and R2. The following table summarizes the requirement and availability of resources.

| Resource | Resource usage per unit of production |  | Amount of resource available |
| :---: | :---: | :---: | :---: |
|  | $\mathbf{P}$ | $\mathbf{Q}$ |  |
| Manpower | 1 | 1 | 10 |
| R1 | 1 | 2 | 18 |
| R2 | 2 | 1 | 18 |

The maximum profit the company can make is
(A) 45
(B) 48
(C) 42
(D) 54

Key: (B)
33. A tool of an NC machine has to move along a circular arc from $(20,20)$ to $(10,10)$, while performing an operation. The centre of the arc is at $(20,10)$. Which one of the following NC tool commands performs the above mentioned operation?
(A) N020 G03 X20 Y20 X10 Y10 R10
(B) N020 G02 X20 Y20 X10 Y10 R10
(C) N0 20 G02 X10 Y10 X20 Y20 R10
(D) N020 G01 X20 Y20 X10 Y10 R10

Key: (A)
34. In a shaft-hole assembly, the hole is specified as $30_{0.000}^{0.040} \mathrm{~mm}$. The mating shaft has a clearance fit with minimum clearance of 0.01 mm . The tolerance on the shaft is 0.3 mm . The maximum clearance in mm between the hole and the shaft is
(A) 0.04
(B) 0.05
(C) 0.08
(D) 0.10

Key: (C)
35. 'GO' and 'NO GO' snap gauges are to be designed for a shaft $36.000_{+0.010}^{+0.070} \mathrm{~mm}$. Gauge tolerance can be taken as $5 \%$ of the hole tolerance. Following the ISO system of gauge design, the respectively size of 'GO' and 'NO GO' gauges are
(A) 36.013 mm and 36.067 mm
(B) 36.015 mm and 36.065 mm
(C) 36.018 mm and 36.062 mm
(D) 36.020 mm and 36.060 mm

Key: (A)
36. A circular tank of 4 m is filled up to a height of 3 m . Assuming almost steady flow and neglecting losses, the time taken in seconds to empty the tank through a 5 cm diameter hole located at the centre of the tank bottom (take acceleration due to gravity $\mathrm{g}=9.81 \mathrm{~m} / \mathrm{s}^{2}$ ) is (round off to the nearest integer)
(A) 5005
(B) 1807
(C) 8097
(D) 3154

Key: (A)
37. The probability mass function $\mathrm{P}(\mathrm{x})$ of a discrete random variable X is given by $\mathrm{P}(\mathrm{x})=\frac{1}{2^{\mathrm{x}}}$, where $\mathrm{x}=1,2, \ldots, \infty$. The expected value of X is $\qquad$ (in integer).

Key: (2)
38. The time to pass through a security screening at an airport follows and exponential distribution. The mean time to pass through the security screening is 15 minutes. To catch the flight, a passenger must clear the security screening within 15 minutes. The probability that the passenger will miss the flight is
$\qquad$ (round off to 3 decimal places).
Key: (0.365-0.370)
39. A machine shop has received four jobs $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D for processing on a single CNC machine. All jobs are available for processing on the first day of the production schedule calendar, and processing times and due dates as applicable on the first day are given below. Using earliest due date rule, the average tardiness (in days) is $\qquad$ (in integer).

| Job | Processing time (in days) | Due date (day) |
| :---: | :---: | :---: |
| A | 8 | 14 |
| B | 5 | 10 |
| C | 7 | 12 |
| D | 9 | 19 |

Key: (4)
40. A time study is carried out for a spot welding operation which is being performed by an operator. The time taken (in seconds) for five observations are recorded as $40,35,45,37$ and 43 , respectively. If the standard time and the allowance for this operation are 45 seconds and 9 seconds, respectively, then the performance rating (in percentage) of the operator is $\qquad$ (in integer)
Key: (90)
41. The initial cost of a machine is INR $10,00,000$ and its salvage value after 10 years of use is INR 50,000 . Using the straight line depreciation method, the book value in INR of the machine at the end of $7^{\text {th }}$ year is $\qquad$ (in integer).
Key: (335000)
42. A project consists of eight activities. The time required for each activity and its immediate predecessor(s) are given in the table below.

| Activity | Activity time (in days) | Immediate predecessor (s) |
| :---: | :---: | :---: |
| A | 2 | - |
| B | 3 | - |
| C | 2 | A |
| D | 4 | A, B |
| E | 4 | C |
| F | 3 | C |
| G | X | D, E |
| H | 2 | F, G |

If the project completion time using critical path method (CPM) is 15 days, then the value of X (in days) is $\qquad$ (in integer)

Key: (5)
43. A wire of 5 mm diameter is drawn into a wire of 4 mm diameter through a conical die at a constant pulling speed of $5 \mathrm{~m} / \mathrm{s}$. Neglecting the coefficient of friction and redundant work, the drawing stress $\left(\sigma_{d}\right)$ in MPa for the above process is given by $\sigma_{d}=\bar{\sigma} \ell n\left[\frac{1}{1-r}\right]$, where $\bar{\sigma}$ is the mean flow strength of wire material in MPa, and $r$ is the ratio of decrease in area of cross-section to initial area of cross-section of the wire. If the mean flow strength of wire material is 600 MPa , then the power required in kW in the above wire drawing process is $\qquad$ . (round off to 2 decimal places)
Key: (16.8-16.84)
44. In an arc welding process, the DC power source characteristics is linear with an open circuit voltage of 60 V and short current of 600 A . The heat required for melting a metal during the welding is $10 \mathrm{~J} / \mathrm{mm}^{3}$, and the heat transfer and melting efficiencies are $80 \%$ and $25 \%$, respectively. If the weld cross-sectional area of $20 \mathrm{~mm}^{2}$ is made using the maximum are power, then the required welding speed $\mathrm{mm} / \mathrm{s}$ is
$\qquad$ (round off to one decimal place).

Key: (8.8-9.2)
45. A company is producing a disc-shaped product of 50 mm thickness and 1.0 m diameter using sand casting process. The solidification time of the above casting process is estimated by Chvorinov's equation $t=B\left[\frac{V}{A}\right]^{2}$, where $B$ is the mold constant, and $V$ and $A$ are the volume and surface area of the casting, respectively. It is decided to modify both the thickness and diameter of the disc to 25 mm and 0.5 m , respectively, maintain the same casting condition. The percentage reduction in solidification time of the modified disc as compared to that of the bigger disc is $\qquad$ (round off to one decimal place).
Key: (74.5-75.5)
46. A single point cutting tool with $15^{\circ}$ orthogonal rake angle is used to machine a mild steel plate under orthogonal machining condition. The depth of cut (uncut thickness) is set at 0.9 mm . If the chip thickness is 1.8 mm , then the shear angle degree is $\qquad$ (rounded off to one decimal place).

Key: (28-30)
47. The top layer of a flat $750 \mathrm{~mm} \times 300 \mathrm{~mm}$ rectangular mild steel plate is to be machined with a single depth of cut using a shaping machine. The plate has been fixed by keeping 750 mm side along the tool travel direction. If the approach and the over-travel are 25 mm each, average cutting speed is $10 \mathrm{~m} / \mathrm{min}$, feed rate is $0.4 \mathrm{~mm} / \mathrm{stroke}$, and the ratio of return time to cutting time of the tool is $1: 2$, the time (in minutes) required to complete the machining operation is $\qquad$ (round off to one decimal place).
Key: (89-91)
48. A 3 mm thick steel sheet, kept at room temperature of $30^{\circ} \mathrm{C}$, is cut by a fibre laser beam. The laser spot diameter on the top surface of the sheet is 0.2 mm . The laser absorptivity of the sheet is $50 \%$. The properties of steel are density $=8000 \mathrm{~kg} / \mathrm{m}^{3}$, specific heat $=500 \mathrm{~J} / \mathrm{kg} .{ }^{\circ} \mathrm{C}$, melting temperature $=1530^{\circ} \mathrm{C}$, and latent heat of fusion $=3 \times 10^{5} \mathrm{~J} / \mathrm{kg}$. Assume that melting efficiency is $100 \%$ and that the kerf width is equal to the laser spot diameter. The maximum speed (in $\mathrm{m} / \mathrm{s}$ ) at which is equal to the laser spot diameter. The maximum speed (in $\mathrm{m} / \mathrm{s}$ ) at which the sheet can be fully cut at 2 kW laser power is
$\qquad$ $-$

Key: (0.193-0.203)
49. In a point-to-point open-loop NC drive, a stepper motor with $1.8^{\circ}$ step angle is coupled to a leadscrew through a gear reduction of $4: 1$ (4 rotations of the motor enables 1 rotation of leadscrew). The singlestart leadscrew has a pitch of 4 mm . The worktable of the system is driven by the leadscrew. If the table moves at a uniform speed of $10 \mathrm{~mm} / \mathrm{s}$, the pulse frequency (in Hz ) required to drive the stepper motor is
$\qquad$ (round of to one decimal place).


Key: (1999-2001)
50. A 30 kg smooth, solid sphere rests on two frictionless inclines as shown the figure. The magnitude of contact force in N acting at the point A is (take acceleration due to gravity $\mathrm{g}=9.81 \mathrm{~m} / \mathrm{s}^{2}$ and consider both sphere and inclines to be rigid) $\qquad$ (round off to 2 decimal place)


Key: (147)
51. Consider the truss shown in the figure. The members $\mathrm{AB}, \mathrm{BC}$ and CA are all rigid and form an equilateral triangle. The contact between roller and ground at C is frictionless. If the self-weight of members is neglected, the force in member BC in N is (negative sign should be used if the force is compressive and positive if the force in the member is tensile) $\qquad$ (round off to one decimal place).


Key: (-5773.7to -5773.4)
52. A fluid with dynamic viscosity $\mu=1$ Pa.s is flowing through a circular pipe with diameter 1 cm . If the flow rate (discharge) in the pipe is 0.2 liter/s, the maximum velocity in $\mathrm{m} / \mathrm{s}$ of the fluid in the pipe is (assume fully developed flow and take fluid density $\rho=1000 \mathrm{~kg} / \mathrm{m}^{3}$ ) $\qquad$ (round off to one decimal place)

Key: (5.1)
53. Value of function $\mathrm{y}(\mathrm{x})$ at discrete values of x for $0 \leq \mathrm{x} \leq 10$ are given in table. Using trapezoidal rule, $\int_{0}^{10} y(x) d x=$ $\qquad$ (round off to one decimal place).

| x | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{y}(\mathrm{x})$ | 5 | 3 | 0 | -5 | -10 | -6 | 0 | 5 | 11 | 18 | 30 |

Key: (33.5)
54. Temperature field inside a sphere of radius $R=1 \mathrm{~m}$ with origin at its centre is $T(x, y, z)=100-70 x+51 y-80 z-10 x^{2}-20 y^{2}-20 z^{2}$. If thermal conductivity of the sphere material is $\mathrm{K}=50 \mathrm{~W} / \mathrm{m} . \mathrm{K}$ and Fourier law of heat conduction is valid, net heat leaving the sphere per unit time in W is $\qquad$ (round off to one decimal place).

Key: (20943.8-20944.1)
55. A 3.5 mm thick sheet is rolled using a two high rolling mill to reduce the thickness under plane strain condition. Both rolls have a diameter of 500 mm and are rotating at 200 RPM. The coefficient of friction at the sheet and roll interface is 0.08 , and the elastic deflection of the rolls is negligible. If the mean flow strength of the sheet material is 400 MPa , then the minimum possible thickness (in mm) of sheet that can be produced in a single pass is $\qquad$ (round off to 2 decimal places).

Key: (1.9)

